National Recovery and Resilience Plan



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SOFIA UNIVERSITY -MARKING MOMENTUM FOR INNOVATION AND TECHNOLOGICAL TRANSFER



OF THE REPUBLIC OF BULGARIA

# **Advanced Variational Analysis and Applications (AVAA)**

## Research field: Mathematics

M. Krastanov, M. Nikolova, On the small-time local controllability, Systems & Control Letters, 177, art. No. 105535, 2023. WOS:001009329800001

Abstract. A class of polynomial control systems is considered. The local properties of the corresponding reachable sets are studied by using a general differential-geometrical approach based on the Campbell-Baker-Hausdorff formula. The main result is a new sufficient condition of smalltime local controllability. Two four-dimensional

M. Ivanov, S. Troyanski, N. Zlateva, Orlicz functions that do not satisfy the  $\Delta_2$ condition and high order Gateaux smoothness in  $h_M(\Gamma)$ , Proceedings of the AMS, Feb 2024. WOS:001171438300001

Abstract. We study Orlicz functions that do not satisfy the  $\Delta_2$  condition at zero. We prove that for every Orlicz function M such that  $\limsup_{t\to 0}$  $M(t)/t^p > 0$  for some  $p \ge 1$ , there exists a positive sequence  $T=(t_k)$  tending to zero and such that:  $\sup_{k \in \mathbb{N}} M(ct_k)/M(t_k) < \infty, \text{ for all } c > 1,$ 

M. Ivanov, N. Zlateva, Slopes and Moreau-Rockafellar theorem, Journal of Convex Analysis, 2024, accepted.

Abstract. Properties of local and global slopes of a function and its approximate critical points sets are studied in relation to determination of the function.



## examples illustrate this result.



D. Kamburova, R. Marinov, N. Zlateva, Saddle points in completely regular topological spaces, Vietnam Journal of Mathematics, March 2024. WOS:001190451200001

i.e., M satisfies the  $\Delta_2$  condition with respect to T.

Consequently, we show that for each Orlicz function with lower Boyd index  $\alpha_M < \infty$  there exists an Orlicz function N such that:

(a) there exists a positive sequence  $T=(t_k)$  tending to zero such that N satisfies the  $\Delta_2$  condition with respect to *T*, and

(b) the space  $h_N$  is isomorphic to a subspace of  $h_M$  generated by one vector.

We apply this result to find the maximal possible order of Gateaux differentiability of a continuous bump function on the Orlicz space  $h_M(\Gamma)$  for  $\Gamma$ uncountable.



V. Shivarov, **D. Grigorova**, A. Yordanov, Relative risk of death in Bulgarian cancer patients during the initial waves of the COVID-19 pandemic, Healthcare, 11 (18), art. No. 2594, 2023. WOS:001145376500001

Abstract. This study aims to assess whether Bulgarian cancer patients experienced a higher relative risk (RR) of death compared to the general Bulgarian population during the pandemic. The impact of the COVID-19 waves and predominant SARS-CoV-2 variants on RR was evaluated on various cancer types and age groups using a multiple linear regression approach. Surprisingly, the RR of death in cancer patients was lower during pandemic waves.



Abstract. We give a characterization of completely regular topological spaces. Applying some recent results for supinf problems in completely regular topological spaces we establish a variational principle for saddle points. Wellposedness of saddle point problems is studied as well.



H. Topalova, N. Zlateva, **Perturbation method in Orlicz sequence spaces**, Set-Valued and Variational Analysis, 2024, accepted.

**Abstract.** We develop a new perturbation method in Orlicz sequence spaces  $\ell_M$  with Orlicz function M satisfying  $\Delta_2$  condition at zero. This result allows one to support from below any bounded below lower semicontinuous function with bounded support, with a perturbation of the defining function  $\sigma_M$ .



## Research team:

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#### NATIONAL RECOVERY AND RESILIENCE PLAN PART OF THE PROGRAM TO ACCELERATE ECONOMIC RECOVERY AND TRANSFORMATION THROUGH SCIENCE AND INNOVATION